

# Business Statistics

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AUSTRALIA / NEW ZEALAND EDITION 6

### CENGAGE Learning

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## Brief contents

1	What is statistics?	1
2	Types of data, data collection and sampling	17
PA	RT 1 DESCRIPTIVE MEASURES AND PROBABILITY	41
З	Graphical descriptive techniques – Nominal data	43
4	Graphical descriptive techniques – Numerical data	82
5	Numerical descriptive measures	128
6	Probability	203
7	Random variables and discrete probability distributions	251
8	Continuous probability distributions	302
PA	RT 2 STATISTICAL INFERENCE	339
9	Statistical inference: Introduction	341
10	Sampling distributions	347
11	Estimation: Describing a single population	369
12	Estimation: Comparing two populations	421
13	Hypothesis testing: Describing a single population	455
14	Hypothesis testing: Comparing two populations	517
15	Inference about population variances	567
16	Analysis of variance	597
17	Additional tests for nominal data: Chi-squared tests	665
18	Simple linear regression and correlation	703
19	Multiple regression	767
20	Model building	825
21	Nonparametric techniques	870
22	Statistical inference: Conclusion	915
PA	RT 3 APPLICATIONS	959
23	Time series analysis and forecasting	961
24	Index numbers	1013
25	Decision analysis – online chapter	25-1

## Contents

Pre	face	xiii
Res	sources guide	xvii
Ack	nowledgements	xxiii
Abo	out the authors	xxiv
1	What is statistics?	1
	Introduction to statistics	2
	1.1 Key statistical concepts	4
	1.2 Practical applications	5
	Case 3.6 Differing average weekly earnings of men and women in Australia	6
	Case 5.9 Aussies and Kiwis are leading in education	6
	Case 15.1 Comparing salary offers for finance and marketing MBA majors - I	6
	Case 17.1 Gold lotto	7
	Case 18.1 Does unemployment affect the average hourly	_
	earnings of New Zealanders?	/
	1.3 How managers use statistics	8
	1.4 Statistics and the computer	9 10
	Appendix 1.A Introduction to Microsoft Eycel	10
0		47
	Types of data, data collection and sampling	17
	Introduction	18
	2.1 Types of data	19
	2.2 Methods of collecting data	24 00
	2.3 Sampling	20 20
	2.5 Sampling and non-sampling errors	30
	Summary	39
	Summary	00
ΡA	RT 1 DESCRIPTIVE MEASURES AND PROBABILITY	41
3	Graphical descriptive techniques – Nominal data	43
	Introduction	44
	3.1 Graphical techniques to describe nominal data	45
	3.2 Selecting a chart: Which chart is best?	53
	3.3 Graphical techniques to describe ordinal data	59
	3.4 Describing the relationship between two nominal variables	67
	Summary	73
	Case 3.1 Road fatalities in Australia by state	/6 
	Lase 3.2 Corporate tax rates around the world	//
	Case 3.4 Where is the diverse rate bacding?	8/ סכ
	Case 3.5 Coographic location of chang expension in Australia	70 70
	Case 5.5 Geographic location of share ownership in Australia	79

	Case 3.6 Differing average weekly earnings of men and women in Australia	79
	Case 3.7 The demography of Australia	79
	Case 3.8 Survey of graduates	80
	Case 3.9 Overseas student contributions to Australian educational institutions	81
	Case 3.10 Is the Australian overseas student market on the decline?	81
4	Graphical descriptive techniques – Numerical data	82
	Introduction	83
	4.1 Graphical techniques to describe numerical data	83
	4.2 Describing time-series data	104
	4.3 Describing the relationship between numerical two variables	108
	4.4 Graphical excellence and deception	116
	Summary	124
	Case 4.1 The question of global warming	126
	Case 4.2 Economic freedom and prosperity	127
	Case 4.3 An analysis of telephone bills	127
5	Numerical descriptive measures	128
	Introduction	129
	5.1 Measures of central location	130
	5.2 Measures of variability	142
	5.3 Measures of relative standing and box plots	159
	5.4 Approximating descriptive measures for grouped data	167
	5.5 Measures of association	169
	5.6 General guidelines on the exploration of data	185
	Summary	186
	Case 5.1 Return to the global warming question	191
	Case 5.2 Another return to the global warming question	191
	Case 5.3 Performance of major Australian companies	191
	Case 5.4 Consumer income versus expenditure	192
	Case 5.5 The gulf between the rich and the poor – life expectancy and literacy	193
	Case 5.6 Sydney and Melbourne leading the way in the growth in house prices	193
	Case 5.7 Performance of managed funds in Australia – 2-star rated	
	versus 4-star rated funds	194
	Case 5.8 Life in suburbs drives emissions higher	195
	Case 5.9 Aussies and Kiwis are leading in education	196
	Appendix 5.A Summation notation	197
6	Probability	203
	Introduction	204
	6.1 Assigning probabilities to events	204
	6.2 Joint, marginal and conditional probability	215
	6.3 Rules of probability	225
	6.4 Probability trees	231
	6.5 Bayes' law	236
	6.6 Identifying the correct method	243
	Summary	244
	Case 6.1 Let's make a deal	247
	Case 6.2 University admissions in Australia: Does gender matter?	247

	Case 6.3 Maternal serum screening test for Down syndrome	248
	Case 6.4 Levels of disability among children in Australia	248
	Case $6.5$ Probability that at least two people in the same room	
	have the same birthday	249
	Case 6.6 Home ownership in Australia	249
7	Random variables and discrete probability distributions	251
	Introduction	252
	7.1 Random variables and probability distributions	252
	7.2 Discrete probability distributions	254
	7.3 Expected value and variance	261
	7.4 Bivariate distributions	268
	7.5 Applications in finance: Portfolio diversification and asset allocation	274
	7.6 Binomial distribution	281
	7.7 Poisson distribution	290
	Summary	296
	Case 7.1 Is there a gender disparity in cultural and leisure activities	
	involvement of school children'?	299
	Case 7.2 How about a carbon tax on motor vehicle ownership?	300
	Case 7.3 Internet usage by children	300
	Case 7.4 Gains from market timing	301
8	Continuous probability distributions	302
	Introduction	303
	8.1 Probability density functions	303
	8.2 Uniform distribution	306
	8.3 Normal distribution	308
	8.4 Exponential distribution	332
	Summary	337
ΡA	RT 2 STATISTICAL INFERENCE	339
9	Statistical inference: Introduction	341
	Introduction	342
	9.1 Data type and problem objective	342
	9.2 How, when and why of statistical inference	344
	9.3 Systematic approach to statistical inference: A summary	345
10	Sampling distributions	347
	Introduction	348
	10.1 Sampling distribution of the sample mean $ar{X}$	348
	10.2 Sampling distribution of the sample proportion $\hat{p}$	362
	10.3 From here to inference	366
	Summary	367
11	Estimation: Describing a single population	369
	Introduction	370
	11.1 Concepts of estimation	371
	11.2 Estimating the population mean $\mu$ when the population	2,1
	variance $\sigma^2$ is known	373

	11.3 Estimating the population mean $\mu$ when the population	
	variance $\sigma^2$ is unknown	387
	11.4 Estimating the population proportion <i>p</i>	400
	11.5 Determining the required sample size	406
	11.6 Applications in marketing: Market segmentation	412
	Summary	416
	Case 11.1 Estimating average weekly poultry expenditure of New Zealanders	419
	Case 11.2 Cold men and cold women will live longer!	420
	Case 11.3 Super fund managers letting down retirees	420
12	Estimation: Comparing two populations	421
	Introduction	422
	12.1 Estimating the difference between two population means $\mu_{ m 1}$ – $\mu_{ m 2}$	
	when the variances $\sigma_1^2$ and $\sigma_2^2$ are known: Independent samples	423
	12.2 Estimating the difference between two population means $\mu_1 - \mu_2$	
	when the variances $\sigma_1^{\epsilon}$ and $\sigma_2^{2}$ are unknown: Independent samples	430
	12.3 Matched pairs experiments: Dependent samples	440
	12.4 Estimating the difference between two population proportions $p_1 - p_2$	444
	Summary	452
	Case 12.1 Australian newspapers are putting up a fight	454
	Case 12.2 Five-star hotels in reach of backpackers	454
13	Hypothesis testing: Describing a single population	455
	Introduction	456
	13.1 Concepts of hypothesis testing	457
	13.2 Testing the population mean when the variance $\sigma^2$ is known	465
	13.3 The <i>p</i> -value of a test of hypothesis	480
	13.4 Testing the population mean when the variance $\sigma^2$ is unknown	490
	13.5 Calculating the probability of a Type II error	496
	13.6 Testing the population proportion	506
	Summary	513
	Case 13.1 Roy Morgan unemployment index	515
	Case 13.2 New Zealand National-led government gains ground	515
	Case 13.3 The republic debate: What Australian women are thinking	515
	Appendix 13.A Excel instructions	516
14	Hypothesis testing: Comparing two populations	517
	Introduction	518
	14.1 Testing the difference between two population means:	
	Independent samples	518
	14.2 Testing the difference between two population means:	
	Matched pairs experiment	537
	14.3 Testing the difference between two population proportions	548
	Summary	558
	Case 14.1 Will the ALP government be re-elected in 2013?	562
	Case 14.2 Direct and broker-purchased mutual funds	562
	Case 14.3 Consumer confidence in New Zealand	563
	Case 14.4 New Zealand Government bond yields: short term	
	versus long term	564

	Case 14.5 The price of petrol: city versus country town	564
	Case 14.6 Student surrogates in market research	565
	Appendix 14.A Excel instructions	566
15	Inference about population variances	567
	Introduction	568
	15.1 Inference about $\sigma^2$	568
	15.2 Inference about $\sigma_1^2/\sigma_2^2$	581
	Summary	594
	Case 15.1 Comparing salary offers for finance and marketing	
	MBA majors – I	595
	Case 15.2 Comparing salary offers for finance and marketing	
	MBA majors – II	595
	Case 15.3 Risk of an asset: Five-year bonds versus 10-year bonds	596
16	Analysis of variance	597
	Introduction	598
	16.1 Single-factor analysis of variance: Independent samples (one-way ANOVA)	599
	16.2 Multiple comparisons	621
	16.3 Analysis of variance: Experimental designs	629
	16.4 Single-factor analysis of variance: Randomised blocks (two-way ANOVA)	630
	16.5 Two-factor analysis of variance	644
	Summary	658
	Case 16.1 Top 300 Australian companies	661
	Case 16.2 Effects of financial planning on small businesses	661
	Case 16.3 Diversification strategy for multinational companies	662
	Case 16.4 Comparing three methods of treating childhood ear infections	663
	Case 16.5 Treatment of headaches	663
17	Additional tests for nominal data: Chi-squared tests	665
	Introduction	666
	17.1 Chi-squared test of a multinomial experiment	666
	17.2 Chi-squared test of a contingency table	676
	17.3 Chi-squared test for normality	689
	17.4 Summary of tests on nominal data	695
	Summary	697
	Case 17.1 Gold lotto	701
	Case 17.2 Which diets work?	701
	Case 17.3 How well is the Australian Government managing	
	the asylum seekers affair?	702
18	Simple linear regression and correlation	703
	Introduction	704
	18.1 Model	705
	18.2 Estimating the coefficients	707
	18.3 Error variable: Required conditions	720
	18.4 Assessing the model	722
	18.5 Using the regression equation	736
	18.6 Coefficients of correlation	741
	18.7 Regression diagnostics – I	749

	Summary	758
	Case 18.1 Does unemployment affect the average hourly earnings	704
	of New Zealanders?	764
	Case 18.2 Does domestic market capital inducide stock prices?	765
	Case 18.4. Cengage Learning Australia	705
	Case 18.5. Do higher interest rates reduce the availability of new bousing?	765
	Case 18.6 Market model of share returns	766
	Case 18.7 Life insurance policies	766
19	Multiple regression	767
	Introduction	768
	19.1 Model and required conditions	768
	19.2 Estimating the coefficients and assessing the model	770
	19.3 Regression diagnostics – II	795
	19.4 Regression diagnostics – III (time series)	807
	Summary	818
	Case 19.1 Are lotteries a tax on the poor and uneducated?	823
	Case 19.2 Demand for beer in Australia	823
	Case 19.3 Cengage Learning Australia revisited	823
	Case 19.4 Average hourly earnings in New Zealand	824
	Case 19.5 Testing a more effective device to keep arteries open	824
20	Model building	825
	Introduction	826
	20.1 Polynomial models	826
	20.2 Nominal independent variables	837
	20.3 Applications in human resources: Pay equity	846
	20.4 Logistic regression	851
	20.5 Variable selection methods	858
	20.6 Stepwise regression	861
	20.7 Model building	865
	Summary	867
	Case 20.1 Does the street number of a house matter?	868
	Case 20.2 Track and field performance forecasts	868
21	Nonparametric statistics	870
	Introduction	871
	21.1 Wilcoxon rank sum test	872
	21.2 Sign test and Wilcoxon signed rank sum test	884
	21.3 Kruskal–Wallis test and Friedman test for independent samples	898
	Summary	909
	Case 21.1 HR Information Systems Inc.	913
	Case 21.2 Bank of Commerce customer survey	913
22	Statistical inference: Conclusion	915
	Introduction	916
	22.1 Identifying the correct technique: Summary of statistical inference	916
	22.2 Beyond the statistics subject – the last word	942
	Case 22.1 Do banks discriminate against women business owners? – Part I	953
	Case 22.2 Do banks discriminate against women business owners? - Part II	954

Case 22.3	Effect of the death of key executives on stock market returns	954
Case 22.4	Northern Territory statehood	955
Case 22.5	Graduate survey report	956
Case 22.6	Evaluation of a new drug	956
Case 22.7	Nutrition education programs	957
Case 22.8	Testing a more effective device to keep arteries open	958
Case 22.9	Type A, B and C personalities and job satisfaction and performance	958

### PART 3 APPLICATIONS

23 Time series analysis and forecasting	961
Introduction	962
23.1 Components of a time series	963
23.2 Smoothing techniques	966
23.3 Trend analysis	976
23.4 Measuring the cyclical effect	982
23.5 Measuring the seasonal effect	985
23.6 Introduction to forecasting	994
23.7 Time series forecasting with exponential smoothing	996
23.8 Time series forecasting with regression	999
Summary	1009
Case 23.1 Part-time employed females	1011
Case 23.2 Australian tourism: Bed occupancy, New South Wales (I	NSW) 1012
Case 23.3 Seasonal and cyclical effects in houses constructed in $V$	/ictoria 1012
24 Index numbers	1013
Introduction	1014
24.1 Constructing unweighted index numbers	1015
24.2 Constructing weighted index numbers	1021
24.3 The Australian consumer price index (CPI)	1026
24.4 Using the CPI to deflate wages and GDP	1029
24.5 Changing the base period of an index number series	1033
Summary	1036
Case 24.1 Soaring petrol prices	1040
Case 24.2 Australian road deaths in 2011 the lowest in almost 60	) years 1040
25 Decision analysis – online chapter	25-1
Introduction	25-2
25.1 Decision problem	25-2
25.2 Using additional information	25-8
Summary	25-20
Appendix A: Summary solutions for selected exercises	1041
Appendix B: Tables	1057
Glossary	1083
Index	1089
indox	1000

## Preface

Business is complex and requires effective management to succeed. Managing complexity requires many skills. There are more competitors, more places to sell products and more places to locate workers. As a consequence, effective decision making is more crucial than ever before. On the other hand, nowadays managers have more access to larger and more detailed data that are potential sources of information for making well-informed objective decisions. However, to achieve this, potential managers need to know which statistical techniques they should use to extract useful information from the data available to them and make informed decisions. For students preparing for the business world, it is not enough to focus merely on mastering a diverse set of statistical techniques and calculations. A course and its recommended textbook must provide a complete picture of statistical concepts and their applications to the real world. *Business Statistics – Australia and New Zealand* is designed to demonstrate that statistical methods are vital tools for today's businesses and managers to improve their decision-making skills.

This book is a thorough Australasian adaptation of the most popular and best-selling United States (US) text, *Statistics for Management and Economics* (9th edition) by Gerald Keller. This edition is a further attempt to make the basic business and economics statistics subject a more effective and enjoyable learning experience for both instructors and students at Australasian universities. It uses familiar local terminology, together with examples, exercises and cases which draw upon Australasian data. To enhance flexibility, we have also rearranged a number of chapters from the US edition. For example, we have incorporated the data collection chapter with types of data at the start of the book, introduce estimation and hypothesis testing in separate chapters, present inference about population variance in another chapter and single population and two or more populations in different chapters. Furthermore, we have included a chapter on index numbers which includes some important topics such as the construction of the Australian Consumer Price Index, as well as comparison of Laspeyres and Paasche index numbers, etc.

When solving problems, *Business Statistics – Australia and New Zealand* uses its unique 'ICI' approach which is renowned for its consistent, proven three-step method to solving problems. The '*Identify, Compute* and *Interpret*' approach teaches you how to determine the appropriate technique, how to compute the statistics and how to interpret the results in the context of the problem at hand. The *compute* stage can be completed either manually (with the aid of a calculator) or using Excel (on the computer), or both.

Today, most subjects use the computer and statistical software or spreadsheets. This book contains step-by-step instructions and commands, with screen images, to teach students how to use Microsoft Excel<sup>®</sup> to solve statistical problems. Additionally, most examples, exercises and cases feature raw data. These data sets are available to download from the **CourseMate for Business Statistics** website, accessible through http://login.cengage.com using the access card that comes with each new copy of this book.

### Key features of our approach

### 1. Systematic approach

This edition retains the systematic approach introduced in the US edition, which teaches students how to recognise which statistical technique to use. We believe that this skill is

the most important one to develop, yet it is the one students have the greatest difficulty in mastering. As each technique is introduced, we demonstrate how to recognise when its use is appropriate and when it is not. A feature of this approach is the review chapter (Chapter 22) presented in the book that allows students to hone their technique-selection skills. In the review chapter, a flowchart develops the logical process for choosing the correct technique. Our ICI approach divides the solution of statistical problems into three parts: (1) identify the technique; (2) calculate/compute the required sample statistics; and (3) interpret the results. Our focus has been on the first and third parts, as the sample statistics could be produced relatively easily with a computer.

When demonstrating examples, we start the solutions by reviewing the appropriateness of the method to be used. One of the main benefits of our approach is that it allows instructors to de-emphasise mathematical manipulation. Consequently, students can spend more time properly setting up the procedure and interpreting the statistical results, and less time grinding out the arithmetic.

For students without access to a computer and statistical software, we continue to teach how to calculate statistics manually (with the exception of the most complicated procedures), and most exercises can be solved in this way.

### 2. Cases

Recent academic conferences devoted to improving the teaching of applied statistics have advocated the use of cases to help motivate students. In practice, a statistician often has access only to raw data and the correct procedure to employ is not obvious; our approach allows us to offer more realistic applications. In fact, many of the cases are based on real studies that have been reported in newspapers, magazines, journals, on television and at academic conferences. Several from our own consulting projects have also been included. Such applications can motivate students, who unfortunately often believe that statistics is not very relevant to their future careers. We believe that our approach can change these attitudes. More than 80 cases are included in the book. Students are expected to analyse the cases and draw conclusions in the same way as the original authors did. These cases are neither summaries of what a particular statistician did to solve a problem, nor glorified exercises; rather, they give students the opportunity to see for themselves how statistical problem solving works.

### 3. Review chapter

The review chapter is included in the book to help students practise identifying the correct techniques. This chapter reviews all the statistical methods covered in the book and provides exercises and cases that require the use of several different statistical procedures. It, therefore, provides practice in the technique identification skills that are required for statistics exams and, ultimately, in any real-life application of statistics.

### 4. Use of Excel

Because the use of spreadsheets is so widespread, we believe that Microsoft<sup>®</sup> Excel is an important addition to this book. However, spreadsheets are not designed for use as statistical software, although they are increasingly capable in data analysis. Because of this limitation, we offer *Data Analysis Plus*<sup>®</sup> macros and workbooks that can be added to the Excel menu and used to solve sophisticated statistical problems beyond Excel's existing capabilities. Excel macros are created to complement Excel's menu of statistical procedures. All statistical techniques introduced in this book can be calculated using either Excel's *Analysis ToolPak* or

*Data Analysis Plus 9.0*<sup>®</sup> which is compatible with Excel 2010. These macros are available to download from the **CourseMate for Business Statistics** website, accessible through http://login.cengagebrain.com using the access card that comes with each new copy of this book. The CD–ROM also contains Version 7.0 of *Data Analysis Plus*<sup>®</sup> which is compatible with previous versions of Excel.

The Excel spreadsheet package is used extensively and presented consistently throughout the book to calculate sample statistics. Most examples in the chapters present manual and using the computer (Excel) solutions, allowing students to see both methods together and to use the preferred method. This feature provides flexibility, allowing the instructor to decide when manual or computer calculations should be emphasised. Detailed instructions and Excel commands provided for the examples make it easy for instructors and students to make use of the computer. They also eliminate the need for instructors to teach how to use the software.

Data files are provided in Excel format for most of the examples, exercises and cases. The sixth edition includes hundreds of data files, some consisting of thousands of observations, which emphasise a central theme in the book – statistical techniques convert data into information. For students who will conduct statistical analyses manually, we have also provided the summary statistics (e.g. means and variances) for exercises, allowing most exercises to be solved manually.

### 5. Exercises

There are over 1500 exercises of varying levels of difficulty. At the end of most sections we supply, under the heading 'Learning the techniques', exercises that help students to learn the arithmetic involved in a specific procedure. 'Applying the techniques' exercises then stress when and why the technique is used and how the results assist in the decision-making process. 'Computer applications' help students gain hands-on experience in applying the techniques to solve problems using real-world data and Microsoft<sup>®</sup> Excel. Supplementary exercises appear at the end of each chapter. As they cover all the topics presented in that chapter, they allow students to practise identifying which of the techniques encountered in that chapter should be employed. They also tend to be more realistic than the other types of exercises.

We are optimistic that the systematic approach used in this book will be successful in helping students to understand how, when and why statistics are used. We hope that the realistic examples, exercises and cases we present, wherever possible with Australasian data, will make the subject more interesting and will persuade students that statistics can play a vital role in managerial decision making.

This text is suitable for a one- or two-semester subject in a business program. Although various sections can be omitted, we strongly urge instructors to attempt to complete most of the statistical inference part of the book. Like a house under construction, the structure of the systematic approach is stronger when most of the various components are in place. Nonetheless, the book has been designed so that chapters can be omitted relatively easily.

### Unique features

- *Chapter opening examples* illustrate the use of techniques introduced in that chapter. These examples are designed to help students learn the concepts in the chapters. These chapter opening examples are revisited at the relevant section of the chapter, where they are solved.
- *Seeing statistics' boxes* refer to applets that are introduced to illustrate statistical concepts visually. They are adapted from *Seeing Statistics* by Gary McClelland and customised to

this text. Nineteen Java applets with a total of 72 applet exercises are available to download from the **CourseMate for Business Statistics** website, accessible through http://login. cengagebrain.com using the access card that comes with each new copy of this book.

- *In addition to the examples provided in each chapter*, in this edition we have included 'Reallife applications' sections which illustrate the fundamental applications of statistics in finance, marketing, human resources management, operations management, accounting and economics.
- *'Key concept' boxes* are included after each technique has been introduced. These boxes will allow students to see a technique's essential requirements, in addition to giving them a way to easily review their understanding. This will be further enhanced by the summary flowchart presented in the review chapter.
- *Several new exercises are added to each chapter.* In particular, new applied exercises are added to the chapter on probability to help students visualise and understand concepts.
- *Several new data sets* have been added to the existing computer exercises section of each chapter. For those students who wish to solve the computer exercises containing data sets manually, summary statistics to these data sets are provided within each exercise.
- *Improved and expanded Data Analysis Plus<sup>®</sup> add-ins for Excel* have been incorporated.
- *In addition to the applets,* we have included several Excel workbooks that feature worksheets for confidence interval estimators and test statistics. By changing one or more inputs, students can learn, for example, the effect of increasing sample sizes on confidence intervals or on test statistics.
- Appendix A: Summary solutions for selected exercises is available in the book.

## Resources guide

As you read this text you will find a number of features in every chapter to enhance your study of **Business Statistics 6e** and help you understand how the theory is applied in the real world.

**Part opening paragraphs** introduce the chapters in each Part to give you an overview of how the chapters relate to each other.

**Learning objectives** give you a clear sense of what each chapter will cover and what you should be able to do after reading the chapter.



**Chapter outlines** at the start of each chapter demonstrate the key concepts that will be covered.



**Real World Examples** are used at the beginning of every chapter. They highlight a specific problem that can be solved using the statistical techniques that will be covered in the chapter. The problem is answered later in the chapter.

**Margin definitions** are key terms, which are defined and included in the margins for easy reference.



**Interesting Examples** are used throughout each chapter. These are designed to teach you to use the authors' unique three-step approach to problem solving, and to help you apply statistics to real business problems.



You will learn to:

- **identify** the right statistical technique to use by focusing on the relationship between the problem and data type
- compute the answer either by hand calculation, or by calculating it in Microsoft Excel® when you see a 'Using the computer' heading with instructions and 'commands' boxes, which included step-by-step instructions on how to complete the examples using Microsoft Excel®
- **interpret** the answer in the context of the problem.

**Factors that identify** boxes are included after each technique has been introduced to allow you to appreciate a technique's essential requirements, and to enable you to review your understanding of each technique.





**Data files**, highlighted throughout the text, enable you to complete the examples, exercises and case studies in the text without having to spend time inputting raw data. These data files are available on the accompanying **CourseMate for Business Statistics** website (http://login.cengagebrain.com). The text contains over 1500 **exercises**, located at the end of each section in chapters.

These include:

- Learning the techniques: exercises that help you to learn the arithmetic involved in a specific procedure.
- Applying the technique: exercises that highlight when and why the techniques are used and how the results assist in the decision-making process.
- **Computer applications:** help you gain hands-on experience in applying the techniques to solve problems using real world data and Microsoft Excel<sup>®</sup>.



Real-Life Applications features are included throughout the text to demonstrate real-world applications of statistics in the areas of finance, marketing, human resource management, accounting and economics.

**Commands** boxes can be found in chapters and include step-by-step instructions on how to complete exercises in Microsoft Excel®.

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Seeing statistics boxes also appear throughout the text. These direct you to the accompanying CourseMate for Business Statistics website (http://login. cengagebrain.com) where you can view applets, which enhance your comprehension by providing visual insight into statistical concepts.

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At the end of each chapter you will find:

- a summary section that consolidates your knowledge of the content of the chapter by reviewing key concepts and drawing out their wider significance,
- a recap of relevant **symbols**,

- a summary of formulas from the chapter, and
- a list of **important terms**.

**Supplementary exercises** at the end of each chapter give you the opportunity to further test your understanding of the key concepts covered.

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**Case studies** are included at the end of each chapter to assist you in applying the statistical techniques you are learning to real-world problems

**Appendices** throughout the text included stepby-step instructions on how to perform complex statistical calculations.





### **Online resources**

Visit http://login.cengagebrain.com and login using the code card in the front of this text for a 12-month access to the *Business Statistics 6e* **CourseMate** website. You'll find interactive self-assessments, quizzes, glossary, flashcards, crosswords, case questions, and more tools to help you excel in your studies.

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### PowerPoint<sup>™</sup> presentations

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#### APLIA



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Online homework has never been easier! APLIA is the perfect solution for your homework management needs, with assignable questions and an online gradebook. Once set up by instructors, students can access additional online review questions related to the text.

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## What is statistics?

### LEARNING OBJECTIVES

This chapter provides an introduction to the two general bodies of methods that together constitute the subject called statistics: descriptive statistics and inferential statistics.

At the completion of this chapter, you should be able to:

describe the two major branches of statistics – descriptive statistics and inferential statistics

understand the key statistical concepts – population, sample, parameter, statistic and census

provide examples of practical applications in which statistics have a major role to play

understand how statistics are used by business managers

understand the basics of the computer spreadsheet package Microsoft Excel and its capabilities in aiding with statistical data analysis for large amounts of data.

### CHAPTER OUTLINE

Introduction to statistics

- 1.1 Key statistical concepts
- 1.2 Practical applications
- 1.3 How managers use statistics
- 1.4 Statistics and the computer
- 1.5 Online resources

### Census in Australia

Information (or data) gathering on various characteristics of different populations of interest are an important part of statistics. When we use all units of the population to record information about the characteristics of interest, this type of data gathering is called a census. Due to cost and other



resource implications, census of the whole population is done only every five years in Australia. The peak Australian government statistics agency, the *Australian Bureau of Statistics*, carries out the census, the two latest being conducted in 2006 and 2011. A census provides a snapshot of the population characteristics in the year it is held. We will discuss census and other forms of data collection in detail in this chapter.

### Introduction to statistics

Today we have access to more data than ever, through the ever-increasing use of information technology to make informed decisions. Statistics is a body of principles and methods concerned with extracting useful information from a set of data to help people make decisions. The role of this book is to describe how, when and why managers and statisticians conduct statistical procedures. Such description is important as you come across different kinds of information and data to which you need to apply different statistical procedures.

In general, statistics can be subdivided into two basic areas: *descriptive statistics* and *inferential statistics*.

### Descriptive statistics

**Descriptive statistics** deals with methods of organising, summarising and presenting data in a convenient and informative form. One form of descriptive statistics uses graphical techniques, which allow statistics practitioners to present data in ways that make it easy for the reader to extract useful information. The main attraction of a graphical presentation is that the message can be easily understood by any layperson. In Chapters 3 and 4 we will present a variety of graphical methods.

Another form of descriptive statistics uses numerical techniques to summarise data. One such method you would have already used frequently is calculating an average or mean. Chapter 5 introduces several numerical statistical measures that describe different features of the data.

The actual technique we use depends on what specific information we would like to extract. Consider the use of descriptive statistics in the following examples.

### EXAMPLE 1.1 ] 4 74 74 1 1 7 7 4 10

### **Business statistics marks**

A student enrolled in a business program is attending his first lecture of the compulsory business statistics course. The student is somewhat apprehensive because he believes the myth that the course is difficult. To alleviate his anxiety, the student asks the lecturer about last year's exam marks of the business statistics course. Because, like all statistics lecturers, this one is friendly and helpful, he obliges and provides a list of the final marks. The marks are composed of all the within-semester assessment items plus the end-of-semester final exam. What information can the student obtain from the list?

This is a typical statistics problem. The student has the data (marks) and needs to apply statistical techniques to get the information he requires. This is a function of *descriptive statistics*.

In this example, we can see at least three important pieces of information. The first is the 'typical' mark. We call this a *measure of central location*. The average is one such measure. In Chapter 5 we will introduce another useful measure of central location, the median. In the above example, the median is the middle mark of the class when the marks are arranged in

#### descriptive statistics

Methods of organising, summarising and presenting data in ways that are useful, attractive and informative to the reader. ascending or descending order. That is, there are 50% of the students who obtained marks less than the median mark, while 50% received marks greater than the median value.

Suppose the student was told that the average mark last year was 67. Is this enough information to reduce his anxiety? The student would likely respond 'no' because he would like to know whether most of the marks were close to the average mark of 67 or were scattered far below and above the average. He needs a *measure of variability*. The simplest such measure is the *range* (discussed further in Chapter 5), which is calculated by subtracting the smallest number from the largest. Suppose the largest mark is 96 and the smallest is 24, then the range is (96 - 24 =) 72. Unfortunately, this provides little information as the range doesn't say where most of the marks are located. Whether most data are located near 24 or near 96 or somewhere in the middle, the range is still 72. We need other measures of variability such as the variance and standard deviation, to reflect the true picture of the spread of the data, which will be introduced in Chapter 5. Moreover, the student must determine more about the marks. In particular he needs to know how the marks are distributed between 24 and 96. The best way to do this is to use a graphical technique, the histogram, to be introduced in Chapter 4.

### EXAMPLE 1.2

### Comparing weekly sales between two outlets

A fast-food franchiser wishes to compare the weekly sales level over the past year at two particular outlets. Descriptive statistical methods could be used to summarise the actual sales levels (perhaps broken down by food item) in terms of a few numerical measures, such as the average weekly sales level and the degree of variation from this average that weekly sales may undergo. Tables and charts could be used to enhance the presentation of the data so that a manager could quickly focus on the essential differences in sales performance at the two outlets.

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There is much more to statistics, however, than these descriptive methods. Decisionmakers are frequently forced to make decisions based on a set of data that is only a small subgroup (sample) of the total set of relevant data (population).

### Inferential statistics

**Inferential statistics** is a body of methods for drawing conclusions (i.e. making inferences) about characteristics of a population, based on information available in a sample taken from the population. The following example illustrates the basic concepts involved in inferential statistics.

### EXAMPLE 1.3

### Profitability of a new life insurance policy

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An Australia-wide automobile club (consisting of about 2 million members) is contemplating extending its services to its members by introducing a new life insurance policy. After some careful financial analysis, the club has determined that the proposed insurance policy would break even if at least 10% of all current members subscribing to the club also purchase the policy. The question here is how can inferential statistics be used by the automobile club to make a decision about introducing their new life insurance policy?

To obtain additional information before reaching a decision on whether or not to proceed with the new insurance policy, the automobile club has decided to conduct a survey of 500 randomly selected current

#### inferential statistics

L01.3

Methods used to draw conclusions about a population based on information provided by a sample of the population.

LO1-4

members. The collection of all its current 2 million or so members is called the *population*. The 500 members selected from the entire population for the analysis are referred to as a *sample*. Each member in the sample is asked if they would purchase the policy if it were offered at some specified price. Suppose that 60 of the members in this sample reply positively. While a positive response by 60 out of 500 members (12%) is encouraging, it does not assure the automobile club that the proposed insurance policy will be profitable. The challenging question here is how to use the response from these 500 sampled members to conclude that at least 10% of all 2 million or so members would also respond positively. The data are the proportion of positive response among the 500 members in the sample. However, we are not so much interested in the response of the 500 members as we are in knowing what the response would be from all of the club's current members. To accomplish this goal we need another branch of statistics – *inferential statistics*.

If the automobile club concludes, based on the sample information, that at least 10% of all its members in the population would purchase the proposed insurance policy, the club is relying on inferential statistics. The club is drawing a conclusion, or making a statistical inference, about the entire population of its 2 million or so members on the basis of information provided by only a sample of 500 members taken from the population. The available data tell us that 12% of this particular sample of members would purchase; the inference that at least 10% of all its members would purchase the new insurance policy may or may not be correct. It may be that, by chance, the club selected a particularly agreeable sample and that, in fact, no more than 5% of the entire population of members would purchase.

Whenever an inference is made about an entire population on the basis of evidence provided by a sample taken from the population, there is a chance of drawing an incorrect conclusion. Fortunately, other statistical methods allow us to determine the reliability of the statistical inference. They enable us to establish the degree of confidence we can place in the inference, assuming the sample has been properly chosen. These methods would enable the automobile club in Example 1.3 to determine, for example, the likelihood that less than 10% of the population of its members would purchase, given that 12% of the members sampled said they would purchase. If this likelihood is deemed small enough, the automobile club will probably proceed with its new venture.

### **1.1** Key statistical concepts

Statistical inference problems involve three key concepts: the population, the sample and the statistical inference. We now discuss each of these concepts in more detail.

### Population

A **population** is the group of all items of interest to a statistics practitioner. It is frequently very large and may, in fact, be infinitely large. In the language of statistics, the word *population* does not necessarily refer to a group of people. It may, for example, refer to the population of diameters of ball bearings produced at a large plant. In Example 1.3, the population of interest consists of all 2 million or so members.

A descriptive measure of a population is called a **parameter**. The parameter of interest in Example 1.3 was the proportion of all members who would purchase the new policy.

### Sample

A **sample** is a subset of data drawn from the population. In Example 1.3, the sample of interest consists of the 500 selected members.

#### population

The set of all items of interest.

#### parameter

A descriptive measure of a population.

#### sample

A set of data drawn from the studied population.

#### statistic

A descriptive measure of a sample.

A descriptive measure of a sample is called a **statistic**. We use sample statistics to make inferences about population parameters. In Example 1.3, the proportion of the 500 members who would purchase the life insurance policy would be a sample statistic that could be used to estimate the corresponding population parameter of interest, the population proportion. Unlike a parameter, which is a constant, a statistic is a variable whose value varies from sample to sample. In Example 1.3, 12% is a value of the sample statistic based on the selected sample.

### Statistical inference

Statistical inference is the process of making an estimate, forecast or decision about a population parameter, based on the sample data. Because populations are usually very large, it is impractical and expensive to investigate or survey every member of a population. (Such a survey is called a census.) It is far cheaper and easier to take a sample from the population of interest and to draw conclusions about the population parameters based on information provided by the sample.

For instance, political pollsters predict, on the basis of a sample of about 1500 voters, how the entire 16 million eligible voters from the Australian population will cast their ballots; and quality control supervisors estimate the proportion of defective units being produced in a massive production process from a sample of only several hundred units.

Because a statistical inference is based on a relatively small subgroup of a large population, statistical methods can never decide or estimate with certainty. Since decisions involving large amounts of money often hinge on statistical inferences, the reliability of the inferences is very important. As a result, each statistical technique includes a measure of the reliability of the inference. For example, if a political pollster predicts that a candidate will receive 40% of the vote, the measure of reliability might be that the true proportion (determined on election day) will be within 3% of the estimate on 95% of the occasions when such a prediction is made. For this reason, we build into the statistical inference a measure of reliability. There are two such measures, the confidence level and the significance level. The *confidence level* is the proportion of times that an estimating procedure would be correct, if the sampling procedure were repeated a very large number of times. For example, a 95% confidence level would mean that, in a very large number of repeated samples, estimates based on this form of statistical inference will be correct 95% of the time. When the purpose of the statistical inference is to draw a conclusion about a population, the *significance level* measures how frequently the conclusion will be wrong in the long run. For example, a 5% significance level means that, in repeated samples, this type of conclusion will be wrong 5% of the time. We will introduce these terms in Chapters 11 and 13.

#### confidence level The degree of

certainty we have that our interval contains the value of the parameter.

#### significance level

The relative frequency of a wrong conclusion.

### **1.2** Practical applications

Throughout the text, you will find examples, exercises and cases that describe actual situations from the business world in which statistical procedures have been used to help make decisions. For each example, exercise or case, you will be asked to choose and apply the appropriate statistical technique to the given data and to reach a conclusion. We cover such applications in accounting, economics, finance, management and marketing. Below is a summary of some of the case studies we have analysed in this textbook with partial data, to illustrate additional applications of inferential statistics. But you will have to wait until you work through these cases in the relevant chapters (where some data is also presented) to find out the conclusions and results.

### Differing average weekly earnings of men and women in Australia

While a lot has been achieved in Australia to reduce the difference between men and women in a number of social status indicators, wage differences are still a matter of concern. The following table presents the average weekly earnings of male and female adults for each Australian state and territory and for Australia as a whole. Present the information using appropriate graphical techniques.

State/Territory	Males	Females
New South Wales	1266.60	843.80
Victoria	1214.60	784.30
Queensland	1270.10	807.40
South Australia	1165.90	762.50
Western Australia	1556.30	834.30
Tasmania	1069.90	742.00
Northern Territory	1419.30	973.20
ACT	1546.50	1172.90
Total (Australia)	1253.10	744.80

### Average weekly (all employees total) earnings (A\$), May 2012

Source: Australian Bureau of Statistics, Average Weekly Earnings, May 2012, cat. no. 6302.0, ABS, Canberra

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### Aussies and Kiwis are leading in education

According to the 2011 published statistics on the human development index (HDI) by the UN, Australians and New Zealanders are leading the world. The HDI is calculated using three indices, namely, education index, GDP index and life expectancy index. The education index data for the top 20, the middle 20 and the bottom 20 of the 176 countries listed in the UN report are recorded. Part of the data are given below. Use suitable numerical summary (central location and variability) measures to analyse the data.

Top 20	Education index	Bottom 20	Education index
Australia	0.993	Eritrea	0.539
Cuba	0.993		
Denmark	0.993		
Finland	0.993	Chad	0.334
New Zealand	0.993	Mali	0.331
		Burkina Faso	0.301
Slovenia	0.969	Niger	0.282

Source: Human Development Report 2009, United Nations Development Program (UNDP), New York, 2011

### Comparing salary offers for finance and marketing MBA majors - I

In the last few years, there has been an increase in the number of web-based companies that offer job placement services. The manager of one such company wanted to investigate the job offers recent MBAs were obtaining. In particular, she wanted to know

ອ . ອ whether finance majors were being offered higher salaries than marketing majors. In a preliminary study, she randomly sampled 50 recently graduated MBAs, half of whom majored in finance and half in marketing. From each she recorded the highest salary offer (including benefits). Can we infer that finance majors obtain higher salary offers than do marketing majors among MBAs? Verify the underlying assumptions.

### Gold lotto

Gold lotto is a national lottery that operates as follows. Players select eight different numbers (six primary and two supplementary numbers) from 1 and 45. Once a week, the corporation that runs the lottery selects eight numbers (six primary and two supplementary numbers) at random from 1 to 45. Winners are determined by how many numbers on their tickets agree with the numbers drawn. In selecting their numbers, players often look at past patterns as a way to help predict future drawings. A regular feature that appears in the newspaper identifies the number of times each number has occurred in the past. The data recorded in the following table appeared in the 20 January 2013 edition of the *Queensland Sunday Mail* after the completion of draw 3287. What would you recommend to anyone who believes that past patterns of the lottery numbers are useful in predicting future drawings?

Lotto number	Number of times drawn	Lotto number	Number of times drawn	Lotto number	Number of times drawn
1	274	16	246	31	252
2	257	17	249	32	256
14	240	29	248	44	230
15	265	30	231	45	242

### Drawing frequency of lotto numbers since draw 413

# Does unemployment affect the average hourly earnings of New Zealanders?

Wages in the labour market are very much influenced by the demand and supply of labour. In any profession or industry, when there is an over supply of labour, the workers will be at a disadvantage and will not be able to demand high wages and vice versa. During the mining boom in Perth, unusually high wages were paid, due to the shortage of workers to work in the mining fields. This has impacted heavily on the other sectors of the economy (e.g. the house prices in Perth were inflated to astonishingly high levels). In New Zealand, also, in the last few decades the average hourly earnings have fluctuated, depending on the state of the economy, especially on the level of labour supply. When the number of unemployed persons increases, it is expected that the average hourly earnings would fall. The data in the file presents the quarterly data for the average hourly earnings and the total number of unemployed persons in New Zealand during the period March 1994 to Sept 2012. Is there any evidence in New Zealand to support the proposition that the higher (lower) the number of unemployed the lower (higher) the average hourly earnings?

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Period	Number unemployed	Average hourly earnings (\$)
Mar. 1994	170300	14.98
Jun. 1994	147000	15.10
Sep. 1994	135800	15.10
Dec. 1994	134800	15.16
Dec. 2011	150700	26.59
Mar. 2012	171 200	26.96
Jun. 2012	156400	27.00
Sep. 2012	170000	27.31

Source: Income Tables, Statistics New Zealand, December 2012

The objective of the problem described in Case 3.6 is to use the descriptive graphical and numerical techniques to analyse the differences in weekly earnings of men and women in Australia; Case 5.9 is to compare the central location and variability of the education index of the top and bottom 20 countries in the world; Case 15.1 is to compare two populations, the variable of interest being the salary of MBA graduates specialising in marketing and finance. Case 17.1 is a day-to-day real-life application. The objective of the problem is to see how statistical inference can be used to determine whether some numbers in a lotto draw occur more often than others. Case 18.1 illustrates another statistical objective. In this case, we need to analyse the relationship between two variables: average hourly earnings and the total number of unemployed persons in New Zealand. By applying the appropriate statistical technique, we will be able to determine whether the two variables are related, and, if so, whether reducing the number of unemployed leads to higher average salary earnings. As you will discover, the technique also permits statistics practitioners to include other variables to determine whether they affect average salary earnings.

### **1.3** How managers use statistics

As we have already pointed out, statistics is about acquiring and using information. However, the statistical result is not the end product. Managers use statistical techniques to help them make decisions. In general, statistical applications are driven by the managerial problem. The problem creates the need to acquire information. This in turn drives the data-gathering process. When the manager acquires data, he or she must convert the data into information by means of one or more statistical techniques. The information then becomes part of the decision process.

Many business students will take or have already taken a subject in marketing. In the introductory marketing subject, students are taught about market segmentation. Markets are segmented to develop products and services for specific groups of consumers. For example, the Coca-Cola Company produces several different cola products.

There is Coca-Cola Classic, Coca-Cola Vanilla, Coca-Cola Zero, Coke, Diet Coke and Caffeine-Free Diet Coke. Each product is aimed at a different market segment. For example, Coca-Cola Classic is aimed at people who are older than 30, Coca-Cola Vanilla is aimed primarily at women, Coke is aimed at the teen market, Diet Coke is marketed towards individuals concerned about their weight or sugar intake, and Caffeine-Free Diet Coke is for

people who are health-conscious. In order to segment the cola market, Coca-Cola had to determine that all consumers were not identical in their wants and needs. The company then had to determine the different parts of the market and ultimately design products that were profitable for each part of the market. As you might guess, statistics plays a critical but not exclusive role in this process.

Because there is no single way to segment a market, managers must try different segmentation variables. Segmentation variables include geographic (e.g. states, cities, country towns), demographic (e.g. age, gender, occupation, income, religion), psycho-graphic (e.g. social class, lifestyle, personality) and behaviouristic (e.g. brand loyalty, usage, benefits sought). Consumer surveys are generally used by marketing researchers to determine which segmentation variables to use. For example, Coca-Cola used age and lifestyle. The age of consumers generally determines whether they buy Coca-Cola Classic or Coke. Lifestyle determines whether they purchase regular, diet or caffeine-free cola. Surveys and statistical techniques would tell the marketing manager that the 'average' Coca-Cola Classic drinker is older than 30, whereas the 'average' Coke drinker is a teenager. Census data and surveys are used to measure the size of the two segments. Surveys would also inform about the number of cola drinkers who are concerned about kilojoules and/or caffeine. The conversion of the raw data in the survey into statistics is only one part of the process. The marketing manager must then make decisions about which segments to pursue (not all segments are profitable), how to sell and how to advertise.

In this book, we will address the part of the process that collects the raw data and produces the statistical result. By necessity, we must leave the remaining elements of the decision process to the other subjects that constitute business programs. We will demonstrate, however, that all areas of management can and do use statistical techniques as part of the information system.

### **1.4** Statistics and the computer

In almost all practical applications of statistics, the statistics practitioner must deal with large amounts of data. In order to calculate various statistical measures, the statistics practitioner would have to perform various calculations on the data; although the calculations do not require any great mathematical skill, the sheer amount of arithmetic makes this aspect of the statistical method time-consuming and tedious. Fortunately, numerous commercially prepared computer programs are available to perform these calculations. In most of the examples used to illustrate statistical techniques in this book, we will provide two methods for answering the question:

- 1 Calculating manually. Except where doing so is prohibitively time-consuming, we will show how to answer the questions using hand calculations (with only the aid of a calculator). It is useful for you to produce some solutions in this way, because by doing so you will gain insights into statistical concepts.
- 2 Using Microsoft Excel. Many business students own a spreadsheet package, and university and TAFE subjects incorporate a spreadsheet into their curriculum. We have chosen to use Microsoft Excel 2010 because we believe that it is and will continue to be the most popular spreadsheet package and is the most accessible package. Excel also comes with a limited statistical tool called Data Analysis. Consequently, we have included (on the CourseMate for Business Statistics website see Section 1.5) a statistical software add-in, Data Analysis Plus 9.0 for Excel 2010 (and Data Analysis Plus 7.0 and 5.1 for earlier versions of Excel), and also created various other macros that can be loaded on to your computer to enable you to use Excel for almost all procedures. Detailed instructions are provided for all techniques. An introduction to the use of Excel is provided in Appendix 1A of this chapter.